Name: _____ Date: ____

Unit 5 – Exponential and Logarithmic Functions – Practice Test

1. The pH of a solution can be described by the equation $pH = -\log[H^+]$, where $[H^+]$ is the hydrogen-ion concentration in moles/litre.

a) The hydrogen-ion concentration in a sample of watermelon is 2.0×10^{-6} moles/litre. Determine the pH of the watermelon, to the nearest tenth.

b) A sample of lemon juice has a pH of 2.1.
Determine the hydrogen-ion concentration of the lemon juice, to four decimal places.

2. The decibel scale measures the intensity of sound. The loudness of a sound, *L* decibels (dB), can be determined using the function $L = 10 \log \left(\frac{I}{I_0} \right)$, where *I* is the intensity of the sound and I_0 is the intensity of the quietest sound that can be detected. Determine the loudness of a sound, in decibels, that is one-fourth as intense as a sound with loudness 60 dB. Give the answer to the nearest whole number.

3. Suppose a student graduates with a student loan of \$17 000. The loan payments are \$220 per month at 2.5% annual interest, compounded monthly. To the nearest month, how long will it take the student to repay the loan? How much interest will they pay?

Pre-Calculus 30 – Unit 5 – Exponential and Logarithmic Functions Practice Test

Name: _	
Date:	

4. Two students each graduate with a student loan of \$15 000 at 2.8% annual interest. Both students make payments totalling \$3588 per year. Student A makes payments of \$299 per month, and the interest is compounded every month. Student B makes payments of \$138 every two weeks, and the interest is compounded every two weeks. Compare the lengths of times it takes each student to repay the loan. Is one payment plan significantly better than the other? Explain.

5. A principal of \$400 is invested at 2% annual interest, compounded quarterly. To the nearest year, when will the amount be \$600?

6. Solve: $125 = 5(3^{x+4})$ Give the solution to the nearest hundredth.

7. Solve: $5^x = 7^{x-2}$ Give the solution to the nearest hundredth.

Pre-Calculus 30 – Unit 5 – Exponential and Logarithmic Functions Practice Test

Name:	
Date:	

8. Solve: $9^{x+1} = 8^{x+2}$ Give the solution to the nearest hundredth.

9. Solve: $\log_2(x+11) - \log_2(x+2) = 1 + \log_2(x-3) - \log_2(x-2)$

10. Solve: $\log(2x - 20) + \log(x - 3) = \log(x - 6) + \log(x - 6)$

11. Determine the equation of the vertical asymptote of the graph of $y = -4 \log_4 (x + 2)$.

- 12. a)Graph $y = -3\log_6(-4(x-1)-5)$ on the grid below.
 - b) Identify the intercepts, the equations of any asymptotes, and the domain and range of the function.



Pre-Calculus 30 – Unit 5 – Exponential and Logarithmic Functions Practice Test

Name:	
Date:	

13, Write as a single logarithm: $\frac{8}{3}\log x + 6\log y$

14. Write this expression in terms of log *a*, log *b*, and log *c*. log $\left(ab^{\frac{7}{4}}c^{5}\right)$

15. Write as a single logarithm: $2\log(x+5) + 2\log(x-7) - \log(x^2 - 2x - 35)$



Sketch its inverse on the same grid. Label the graph with its equation.



Pre-Calculus 30 – Unit 5 – Exponential and Logarithmic Functions Practice Test

Name:	
Date:	

17. Evaluate: $\log_7 \left(49 \sqrt[4]{343} \right)$

18. To the nearest hundreth, estimate the value of $\log_3 5.1$. Show your work, do not evaluate with a calculator.

19. Write 7 as a logarithm with base 2.

- 20. a) Graph $y = \log_6 x$.
- b) Identify the intercepts, the equations of any asymptotes, and the domain and range of the function.



21. Solve: $\left(\frac{1}{16}\right)^{x+4} = \left(\sqrt[3]{256}\right)^x$

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Name: _	
Date:	

22. Solve:
$$\left(\frac{1}{9}\right)^{x} = 3\sqrt[3]{81}$$

23. Solve:
$$\left(\sqrt[3]{5}\right)^{x-5} = \sqrt[4]{125}$$



b) Determine:

.

- i) whether the function is increasing or decreasing
- ii) the intercepts
- iii) the equation of the asymptote
- iv) the domain of the function
- v) the range of the function



25. What are you going to work on better next unit?