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## Unit 5 - Exponential and Logarithmic Functions - Practice Test

1. The pH of a solution can be described by the equation $\mathrm{pH}=-\log \left[\mathrm{H}^{+}\right]$, where $\left[\mathrm{H}^{+}\right]$is the hydrogen-ion concentration in moles/litre.
a) The hydrogen-ion concentration in a sample of watermelon is $2.0 \times 10^{-6} \mathrm{moles} / \mathrm{litre}$. Determine the pH of the watermelon, to the nearest tenth.
b) A sample of lemon juice has a pH of 2.1.

Determine the hydrogen-ion concentration of the lemon juice, to four decimal places.
2. The decibel scale measures the intensity of sound. The loudness of a sound, $L$ decibels ( dB ), can be determined using the function $L=10 \log \left(\frac{I}{I_{0}}\right)$, where $l$ is the intensity of the sound and $I_{0}$ is the intensity of the quietest sound that can be detected. Determine the loudness of a sound, in decibels, that is one-fourth as intense as a sound with loudness 60 dB . Give the answer to the nearest whole number.
3. Suppose a student graduates with a student loan of $\$ 17000$. The loan payments are $\$ 220$ per month at $2.5 \%$ annual interest, compounded monthly. To the nearest month, how long will it take the student to repay the loan? How much interest will they pay?

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4. Two students each graduate with a student loan of $\$ 15000$ at $2.8 \%$ annual interest. Both students make payments totalling $\$ 3588$ per year. Student A makes payments of $\$ 299$ per month, and the interest is compounded every month. Student B makes payments of $\$ 138$ every two weeks, and the interest is compounded every two weeks. Compare the lengths of times it takes each student to repay the loan. Is one payment plan significantly better than the other? Explain.
5. A principal of $\$ 400$ is invested at $2 \%$ annual interest, compounded quarterly.

To the nearest year, when will the amount be $\$ 600$ ?
6. Solve: $125=5\left(3^{x+4}\right)$ Give the solution to the nearest hundredth.
7. Solve: $5^{x}=7^{x-2}$ Give the solution to the nearest hundredth.

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8. Solve: $9^{x+1}=8^{x+2}$ Give the solution to the nearest hundredth.
9. Solve: $\log _{2}(x+11)-\log _{2}(x+2)=1+\log _{2}(x-3)-\log _{2}(x-2)$
10. Solve: $\log (2 x-20)+\log (x-3)=\log (x-6)+\log (x-6)$
11. Determine the equation of the vertical asymptote of the graph of $y=-4 \log _{4}(x+2)$.
12. a)Graph $y=-3 \log _{6}(-4(x-1)-5)$ on the grid below.
b) Identify the intercepts, the equations of any asymptotes, and the domain and range of the function.


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13, Write as a single logarithm: $\frac{8}{3} \log x+6 \log y$
14. Write this expression in terms of $\log a, \log b$, and $\log c . \log \left(a b^{\frac{7}{4}} c^{5}\right)$
15. Write as a single logarithm: $2 \log (x+5)+2 \log (x-7)-\log \left(x^{2}-2 x-35\right)$
16. The graph of $y=\log _{5} x$ is shown below.

Sketch its inverse on the same grid. Label the graph with its equation.


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17. Evaluate: $\log _{7}(49 \sqrt[4]{343})$
18. To the nearest hundreth, estimate the value of $\log _{3} 5.1$. Show your work, do not evaluate with a calculator.
19. Write 7 as a logarithm with base 2.
20. a) Graph $y=\log _{6} x$.
b) Identify the intercepts, the equations of any asymptotes, and the domain and range of the function.

21. Solve: $\left(\frac{1}{16}\right)^{x+4}=(\sqrt[3]{256})^{x}$

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22. Solve: $\left(\frac{1}{9}\right)^{x}=3 \sqrt[3]{81}$
23. Solve: $(\sqrt[3]{5})^{x-5}=\sqrt[4]{125}$
24. a) Use transformations to sketch the graph of the exponential function $y=3^{-3(x-2)}+1$.
b) Determine:
i) whether the function is increasing or decreasing
ii) the intercepts
iii) the equation of the asymptote
iv) the domain of the function
v) the range of the function


